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Dynamic Speed Scaling: Theory and Practice

Carey Williamson

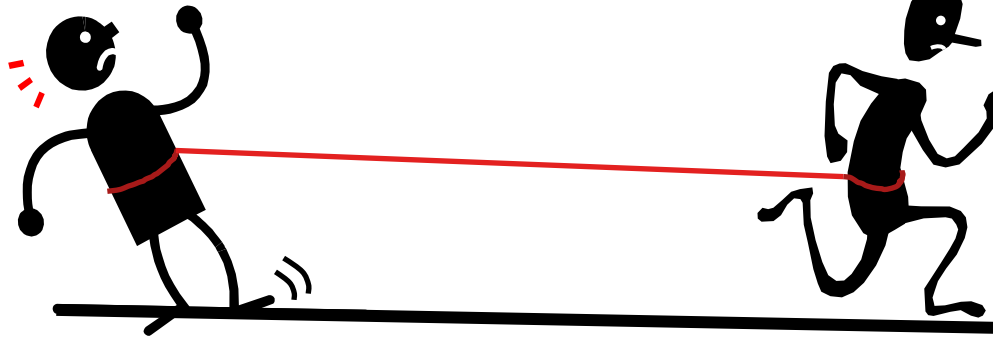
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- The ICT ecosystem is responsible for 10% of the world's energy consumption [Mills 2013]
- Data centers account for roughly 2% of global energy consumption (and still growing at a rate of approximately 6% per annum)
- The most energy-intensive component of any computer is its processor [Skrenes 2016]
 - 90% of energy usage when active (72W/80W)
 - 48% of energy usage when idle (3.1W/6.4W)
- Need for more energy-efficient computing

Speed Scaling: Inherent Tradeoffs

Dynamic Speed Scaling: adapt service rate to the current state of the system to balance energy consumption and performance.

Run
slower:
less
energy



Run
faster:
less
delay

- Minimize power consumption P
 - Minimize energy cost ϵ
 - Minimize heat, wear, etc.
- Minimize response time T
 - Minimize delay
- Maximize job throughput

- There is broad and diverse literature on speed scaling systems for the past 20+ years
- There is a dichotomy between theoretical work and systems work on speed scaling
- Modern processors provide surprisingly rich functionality for speed scaling that is not yet well exploited by systems software
- There are many interesting tradeoffs to explore in dynamic speed scaling systems

- Introduction and Motivation
- Background and Literature Review
- Summary of Key Results and Insights
- Recent Results and Contributions
 - Practice: Experimental Measurements
 - Theory: Autoscaling Effects
- Conclusions and Future Directions

Theoretical Research

- Goal: optimality
- Domains: CPU, parallel systems
- Methods: proofs, complexity, competitive analysis, queueing theory, Markov chains, worst case, asymptotics, simulation
- Metrics: $E[T]$, $E[\epsilon]$, combo, slowdown, competitive ratio
- Power: $P = s^\alpha$ ($1 \leq \alpha \leq 3$)
- Schedulers: PS, SRPT, FSP, YDS
- Speed scalers: job-count-based, continuous and unbounded speeds
- Venues: SIGMETRICS, PEVA, Performance, INFOCOM, OR

Systems Research

- Goal: practicality
- Domains: CPU, disk, network
- Methods: DVFS, power meter, measurement, benchmarking, simulation, power gating, over-clocking, simulation
- Metrics: response time, energy, heat, utilization
- Power: $P = a C_{\text{eff}} V^2 f$
- Schedulers: FCFS, RR, FB
- Speed scalers: threshold-based, discrete and finite speeds
- Venues: SIGMETRICS, SOSP, OSDI, ISCA, MASCOTS, TOCS

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- [Wierman et al. 2009] “Power-Aware Speed Scaling in Processor Sharing Systems”, IEEE INFOCOM

Literature #4: Inexact Job Sizes

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- [Wierman et al. 2008] “Scheduling Despite Inexact Job Size Information”, SIGMETRICS

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- [Snowdon et al. 2007] “Accurate Online Prediction of Processor and Memory Energy Usage under Voltage Scaling”, Embedded Software
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Key Results: Single-Speed World

- PS is the gold standard for fairness
- Asymptotic convergence of slowdown for all work-conserving scheduling policies
- SRPT is “Sometimes Unfair”
- YDS is optimal for energy consumption
- FSP dominates PS for response time

Key Results: Speed Scaling World

- No policy can be optimal, robust, and fair
- Speed scaling exacerbates unfairness
- Asymptotic convergence of slowdown property no longer holds
- FSP's dominance of PS breaks under coupled speed scaling
- FSP's dominance of PS is restored under decoupled speed scaling

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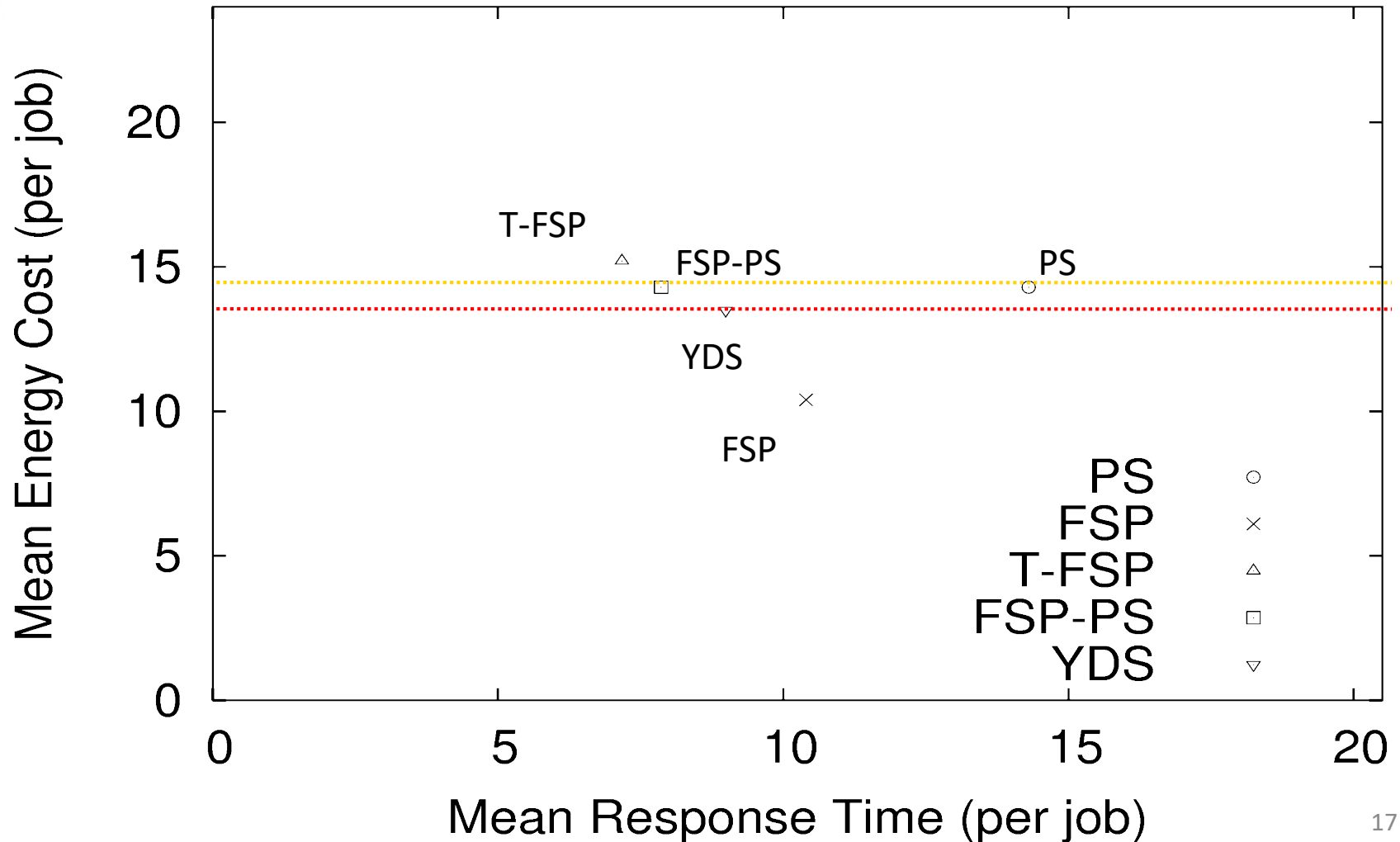
Experimental Calibration and Validation of a Speed Scaling Simulator

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Energy Cost vs Response Time (10 linear jobs; $\alpha = 2$)



- Single-server queue for CPU service
- Single batch of n jobs arrive at time 0
- Job sizes known in advance
- Dynamic speed scaling with $s = f(n)$
- Power consumption $P = s^\alpha$ where $1 \leq \alpha \leq 3$
- Maximum system speed is unbounded
- System speeds are continuous (not discrete)
- Context switches are free (i.e., zero cost)
- Speed changes are free (i.e., zero cost)

Question: How would they perform on real systems?

Bridging Theory and Practice

- Profilo enables all scheduling and speed scaling algorithms to be analyzed on real systems.



Theory

Practice

Profilo Design [Skrenes 2016]

- Flexible framework for the experimental evaluation of arbitrary scheduling and speed scaling policies
- Hybrid user-mode and kernel-mode implementation
- User space: CSV file input to specify workload
- Kernel space: carefully-controlled job execution, timing, and energy measurement using RAPL MSR

P1 5 20
 P2 7 12
 P3 2 50
 P1 1 10
 P4 10 8
 P2 5 30
 ...



1. Process args
2. Set up environment
3. Profiling
4. Summarize results

User space

sysfs API

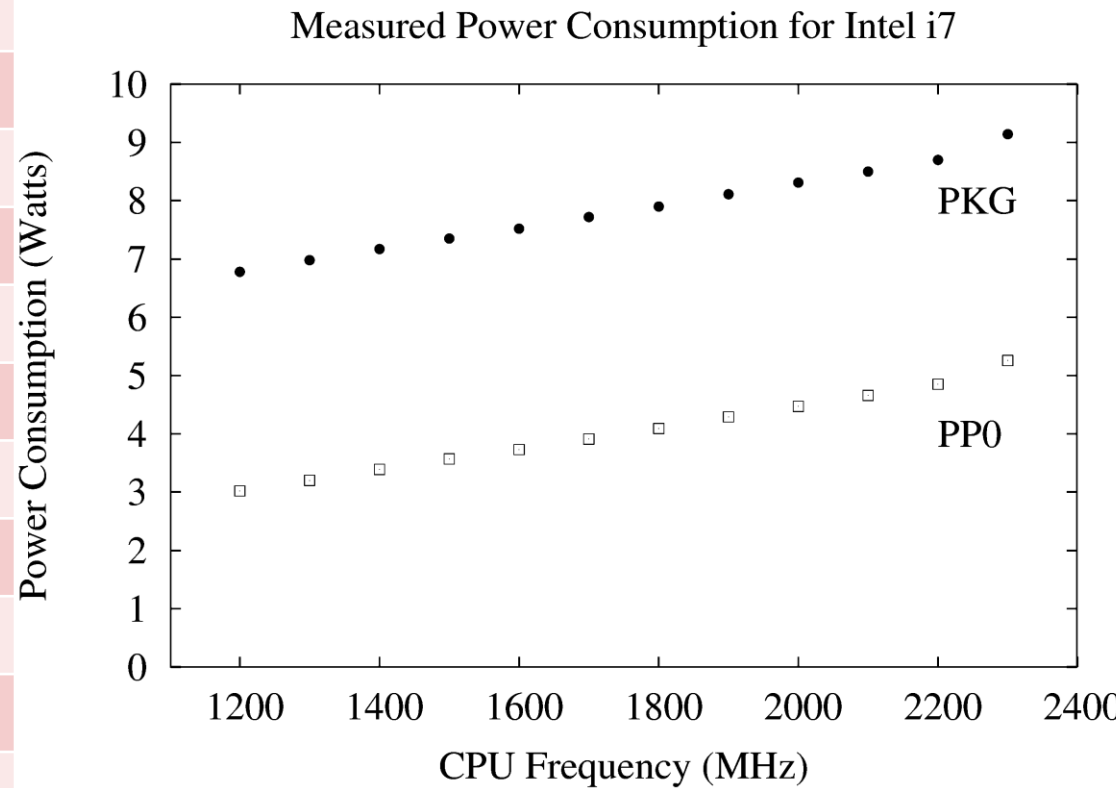
Work unit (primes)
 Do work (loops)
 Sleep busy
 Sleep deep

Kernel space

- Non-architectural model specific registers (MSRs)
- Accurate power meters for each of the domains (independently found to match actual power measurements)
- Four domains (three for any given CPU)
 - Power Plane 0 (PP0)
 - Power Plane 1 (PP1) – Consumer Packages Only
 - DRAM [8], [15] – Server Packages Only
 - Package (PKG)

Frequency (MHz)	PP0 (W)	PKG (W)
2301 (3300)	11.5	15.3
2300	5.4	9.2
2200	5.0	8.9
2100	4.8	8.6
2000	4.6	8.4
1900	4.5	8.3
1800	4.3	8.0
1700	4.1	7.9
1600	3.9	7.6
1500	3.7	7.5
1400	3.5	7.3
1300	3.3	7.1
1200	3.1	6.9

Quite unpredictable and uncontrollable!



Highly linear throughout most of range!

Plus multiple sleep and idle modes (not shown here)

Frequency (MHz)	PPO (W)	PKG (W)	Context Switch (us)
2301 (3300)	11.5	15.3	1.140
2300	5.4	9.2	1.634
2200	5.0	8.9	1.708
2100	4.8	8.6	1.808
2000	4.6	8.4	1.898
1900	4.5	8.3	1.999
1800	4.3	8.0	2.118
1700	4.1	7.9	2.213
1600	3.9	7.6	2.369
1500	3.7	7.5	2.526
1400	3.5	7.3	2.709
1300	3.3	7.1	2.886
1200	3.1	6.9	3.167

Frequency (MHz)	PPO (W)	PKG (W)	Context Switch (us)	Speed Switch (us)
2301 (3300)	11.5	15.3	1.140	0.76
2300	5.4	9.2	1.634	1.09
2200	5.0	8.9	1.708	1.14
2100	4.8	8.6	1.808	1.20
2000	4.6	8.4	1.898	1.26
1900	4.5	8.3	1.999	1.32
1800	4.3	8.0	2.118	1.38
1700	4.1	7.9	2.213	1.47
1600	3.9	7.6	2.369	1.56
1500	3.7	7.5	2.526	1.67
1400	3.5	7.3	2.709	1.81
1300	3.3	7.1	2.886	1.93
1200	3.1	6.9	3.167	2.09

Frequency (MHz)	PPO (W)	PKG (W)	Context Switch (us)	Speed Switch (us)	Mode Switch (ns)
2301 (3300)	11.5	15.3	1.140	0.76	44.8
2300	5.4	9.2	1.634	1.09	64.2
2200	5.0	8.9	1.708	1.14	67.0
2100	4.8	8.6	1.808	1.20	70.2
2000	4.6	8.4	1.898	1.26	73.7
1900	4.5	8.3	1.999	1.32	78.3
1800	4.3	8.0	2.118	1.38	81.9
1700	4.1	7.9	2.213	1.47	86.7
1600	3.9	7.6	2.369	1.56	92.1
1500	3.7	7.5	2.526	1.67	98.6
1400	3.5	7.3	2.709	1.81	105.3
1300	3.3	7.1	2.886	1.93	113.4
1200	3.1	6.9	3.167	2.09	123.1

- Three workloads (each with batch of 12 jobs)
 1. Homogenous
 2. Additive (arithmetic progression)
 3. Multiplicative (factors of 2)

- Three algorithms
 1. PS (epitomizes fairness)
 2. YDS (minimizes power consumption)
 3. FSP-PS (decoupled speed scaling; improves mean response time while retaining fairness)

TABLE III
EXPERIMENTAL RESULTS FOR MEAN RESPONSE TIME $E[T]$ AND ENERGY CONSUMPTION (PP0 AND PKG) (12 JOBS, $\alpha = 1$)

Speed Scaling Policy	Workload 1				Workload 2				Workload 3			
	Time (s)	$E[T]$ (s)	PP0 (J)	PKG (J)	Time (s)	$E[T]$ (s)	PP0 (J)	PKG (J)	Time (s)	$E[T]$ (s)	PP0 (J)	PKG (J)
PS	14.57	14.49	76.80	131.50	46.23	30.10	199.99	372.98	166.15	38.05	562.47	1184.36
FSP-PS	14.57	7.9	76.77	131.60	46.21	16.4	199.41	372.36	166.08	25.7	560.35	1180.83
YDS	14.55	7.9	76.49	130.93	45.80	17.1	198.83	369.88	163.12	27.0	560.94	1170.05

- Observation 1: Decoupled speed scaling (FSP-PS) provides a significant **response time** advantage over PS, for the “same” **energy costs**
- Observation 2: The **response time** advantage of FSP-PS decreases as job size variability increases
- Observation 3: FSP-PS has a slight **energy** advantage over PS because of fewer context switches between jobs
- Observation 4: YDS has the lowest **energy** consumption among these policies (even better than expected due to discretization effect, and no speed changes)

TABLE IV

SIMULATION RESULTS FOR MEAN RESPONSE TIME $E[T]$ AND ENERGY CONSUMPTION (PP0 AND PKG) (12 JOBS, $\alpha = 1$)

Speed Scaling Policy	Workload 1				Workload 2				Workload 3			
	Time (s)	$E[T]$ (s)	PP0 (J)	PKG (J)	Time (s)	$E[T]$ (s)	PP0 (J)	PKG (J)	Time (s)	$E[T]$ (s)	PP0 (J)	PKG (J)
PS	14.4	14.4	75.5	132.4	47.2	29.9	205.1	387.3	167.5	38.4	564.8	1199.0
FSP-PS	14.4	7.8	75.5	132.3	47.2	16.3	205.0	387.3	167.5	25.7	564.8	1199.0
YDS	14.4	7.8	75.5	132.3	46.2	17.5	204.4	383.3	164.5	27.4	562.9	1186.8

- Designed and implemented a novel experimental platform (Profilo) for fine-grain energy measurements
 - Hybrid user-space/kernel-space using RAPL and *hrtimers*
 - Flexible platform to quantify tradeoffs between different scheduling and speed scaling strategies
- Used this experimental platform to do the following:
 - Micro-benchmark a modern Intel processor to measure system costs and power consumption
 - Calibrate/validate a discrete-event simulator for dynamic speed scaling systems
 - Compare and evaluate three different speed scaling strategies from the literature: PS, FSP-PS, and YDS
- Gained new insights into practical aspects of dynamic speed scaling systems

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Autoscaling Effects in Speed Scaling Systems

Maryam Elahi

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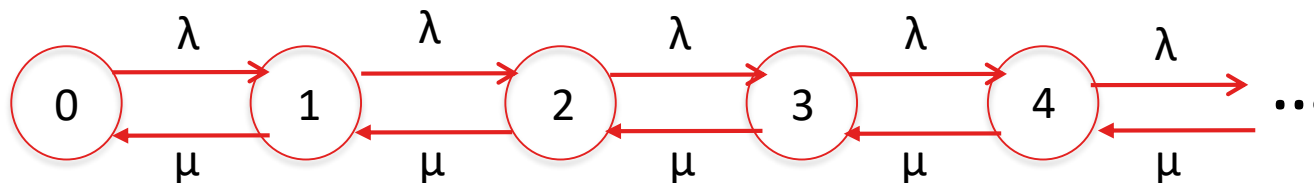
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- Dynamic CPU speed scaling systems
- Service rate adjusted based on offered load
- Classic tradeoff:
 - Faster speed → lower response time, higher energy usage
- Two key design choices:
 - Scheduler: which job to run? (FCFS, PS, FSP, SRPT, LRPT)
 - Speed scaler: how fast to run? (static, coupled, decoupled)
- Research questions:
 - What are the “autoscaling” properties of coupled (i.e., job-count based) speed scaling systems under heavy load?
 - In what ways are PS and SRPT similar or different?

Review: Birth-death Markov chain model of classic M/M/1 queue

Fixed arrival rate λ

Fixed service rate μ



Mean system occupancy: $N = \rho / (1 - \rho)$

Ergodicity requirement: $\rho = \lambda/\mu < 1$

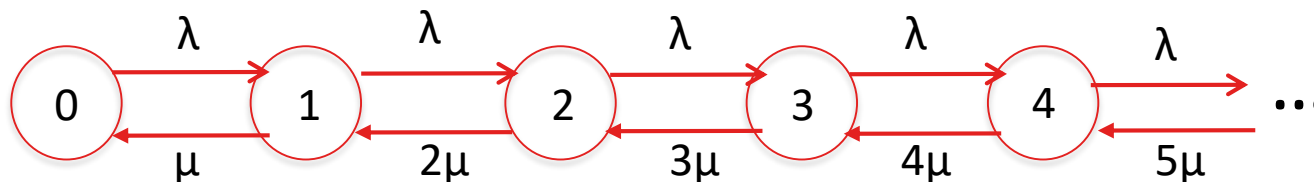
$$p_n = p_0 (\lambda/\mu)^n$$

$$U = 1 - p_0 = \rho$$

Birth-death Markov chain model of classic M/M/∞ queue

Fixed arrival rate λ

Service rate scales linearly with system occupancy ($\alpha = 1$)



Mean system occupancy: $N = \rho = \lambda/\mu$

$$p_n = p_0 \prod_{i=0}^{n-1} (\lambda/(i+1)\mu)$$

System occupancy has Poisson distribution

$$U = 1 - p_0 \neq \rho$$

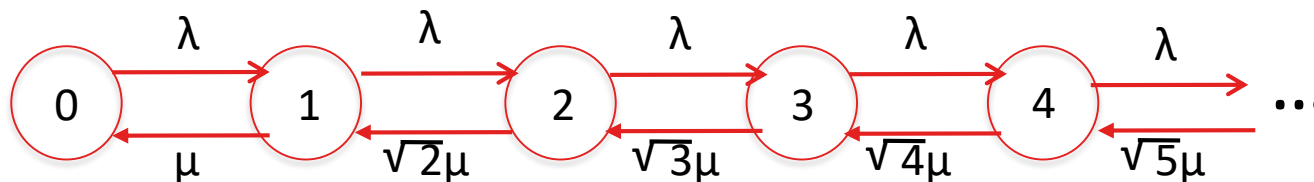
Ergodicity requirement: $\rho = \lambda/\mu < \infty$

FCFS = PS \neq SRPT

Birth-death Markov chain model of dynamic speed scaling system

Fixed arrival rate λ

Service rate scales sub-linearly with system occupancy ($\alpha = 2$)



Mean system occupancy: $N = \rho^2 = (\lambda/\mu)^2$ $p_n = p_0 \prod_{i=0}^{n-1} (\lambda/(\sqrt{i+1})\mu)$

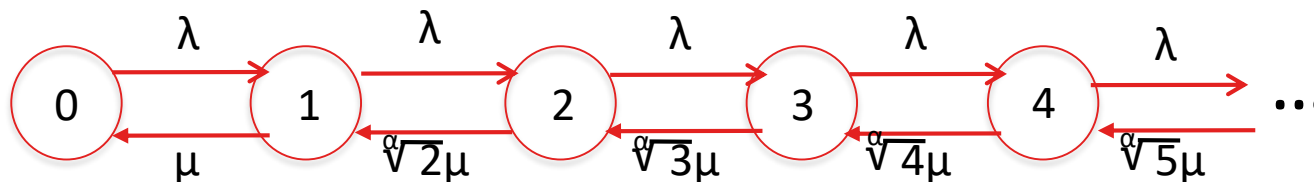
System occupancy has higher variance than Poisson distribution

Ergodicity requirement: $\rho = \lambda/\mu < \infty$

Birth-death Markov chain model of dynamic speed scaling system

Fixed arrival rate λ

Service rate scales sub-linearly with system occupancy ($\alpha > 1$)



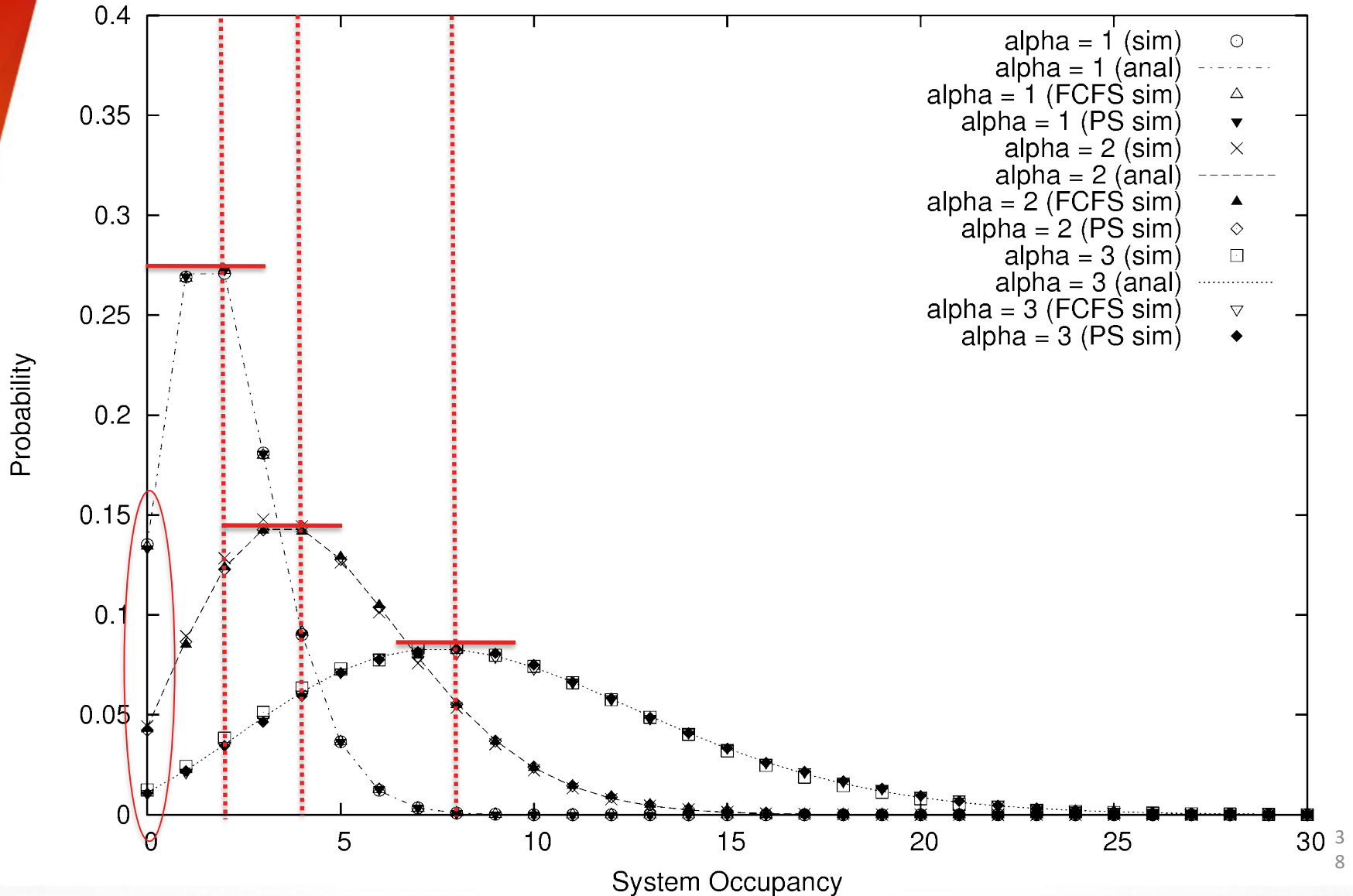
Mean system occupancy: $N = \rho^\alpha = (\lambda/\mu)^\alpha$ $p_n = p_0 \prod_{i=0}^{n-1} (\lambda/(\sqrt{i+1})\mu)$

System occupancy has higher variance than Poisson distribution

Ergodicity requirement: $\rho = \lambda/\mu < \infty$

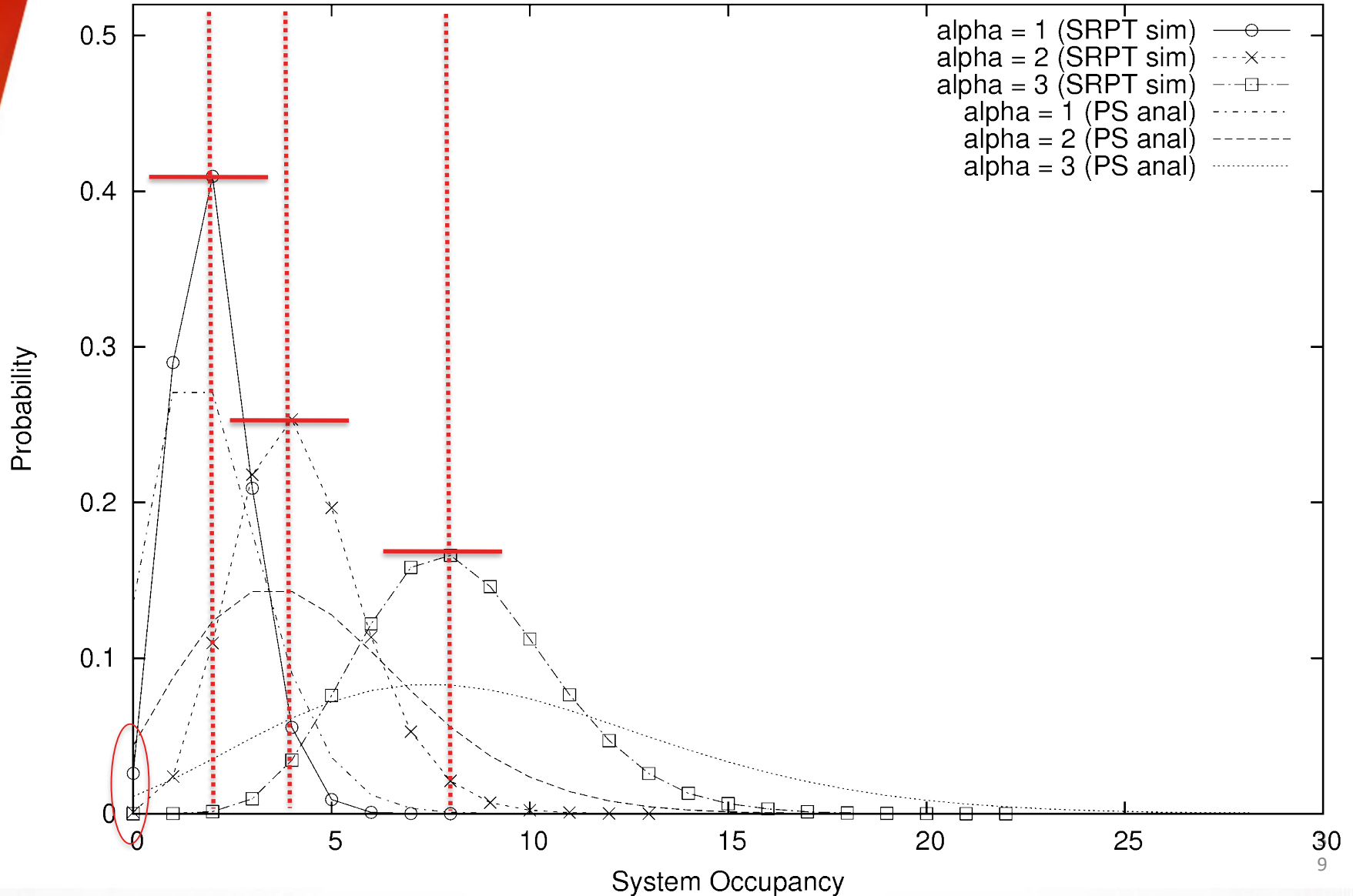
- In speed scaling systems, ρ and U differ
- Speed scaling systems stabilize even when $\rho > 1$
- In stable speed scaling systems, $s = \rho$ (an invariant)
- PS is amenable to analysis; SRPT is not
- PS with linear speed scaling behaves like $M/M/\infty$, which has Poisson distribution for system occupancy
- Increasing α changes the Poisson structure of PS
- At high load, $N \rightarrow \rho^\alpha$ (another invariant property)

Steady-State Probabilities for System Occupancy (Lambda = 2)



SRPT Simulation Results

Steady-State Probabilities for System Occupancy ($\lambda = 2$)



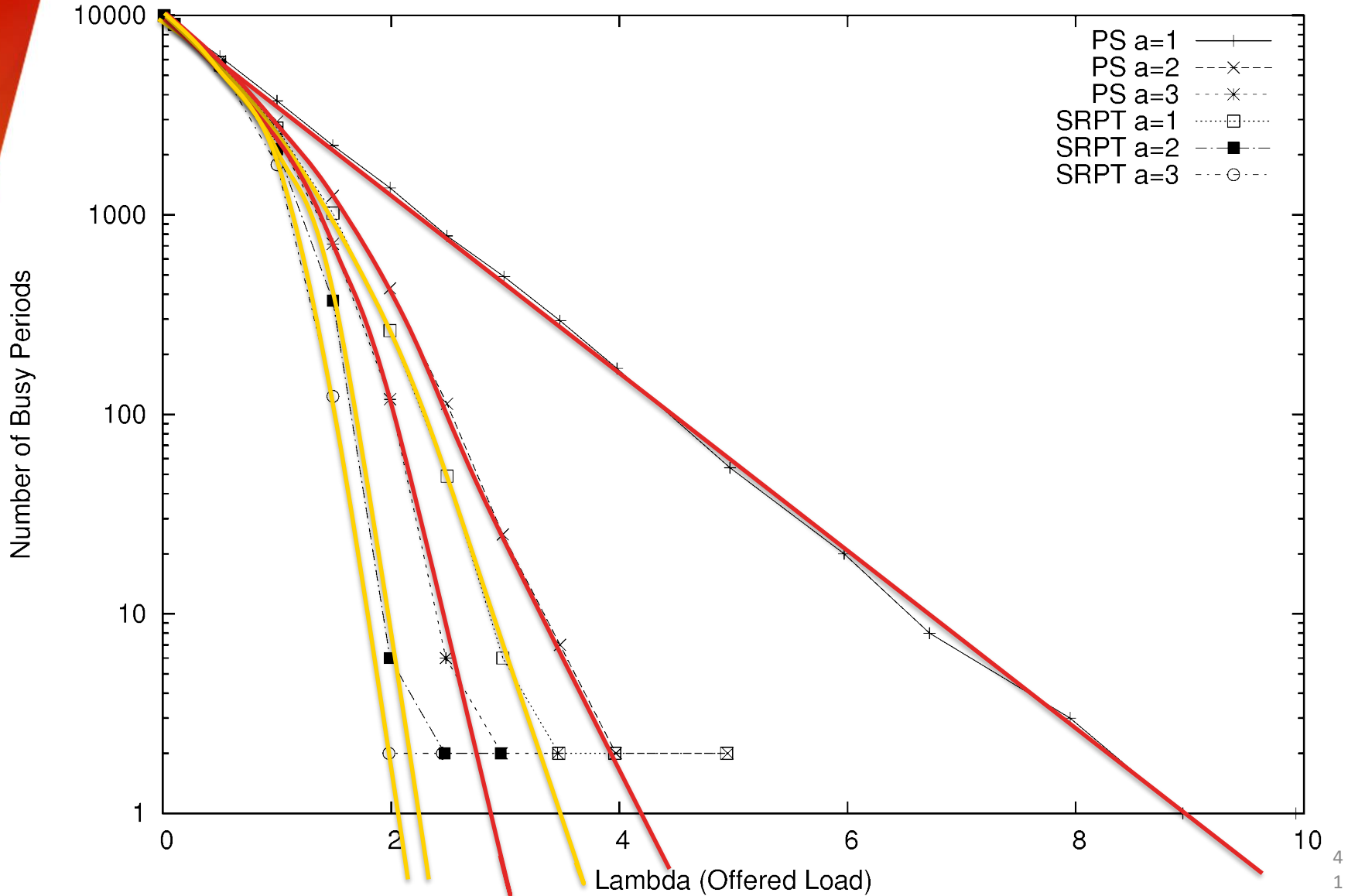
- Similarities:
 - Mean system speed (invariant property)
 - Mean system occupancy (invariant property)
 - Effect of α (i.e., the shift, the squish, and the squeeze)

- Differences:
 - Variance of system occupancy (SRPT is lower)
 - Mean response time (SRPT is lower)
 - Variance of response time (SRPT is higher)
 - PS is always fair; SRPT is unfair (esp. with speed scaling!)
 - Compensation effect in PS
 - Procrastination/starvation effect in SRPT



Busy Period Structure for PS and SRPT (simulation)

Busy Period Characteristics for PS and SRPT



- Under heavy load, busy periods coalesce and $U \rightarrow 1$
- Saturation points for PS and SRPT are different
 - Different “overload regimes” for PS and SRPT
 - Gap always exists between them
 - Gap shrinks as α increases
 - Limiting case ($\alpha = \infty$) requires $\rho < 1$ (i.e., fixed rate)
- SRPT suffers from starvation under very high load
- “Job count” stability and “work” stability differ

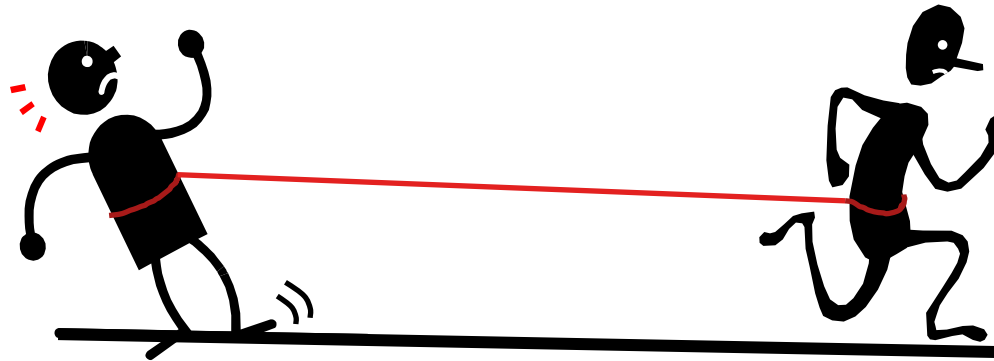
- The autoscaling properties of dynamic speed scaling systems are many, varied, and interesting!
 - Autoscaling effect: stable even at very high offered load ($s = \rho$)
 - Saturation effect: $U \rightarrow 1$ at heavy load, with $N \rightarrow \rho^\alpha$
 - The α effect: the shift, the squish, and the squeeze
- Invariant properties are helpful for analysis
- Differences exist between PS and SRPT
 - Variance of system occupancy; mean/variance of response time
 - Saturation points for PS and SRPT are different
 - SRPT suffers from starvation under very high load
- Our results suggest that PS becomes superior to SRPT for coupled speed scaling, if the load is high enough

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- There is a dichotomy between theoretical work and systems work on speed scaling
- Modern processors provide surprisingly rich functionality for speed scaling that is not yet well exploited by systems software
- There are many interesting tradeoffs to explore in dynamic speed scaling systems

- Cost function for speed scaling optimization
- Redefining the benchmark for fairness
- Stability (or quasi-stability) in overload regimes
- Extending PSBS to speed scaling scenario
- Practical schedulers and speed scalers for modern operating systems that better exploit the available hardware features
- Speed scaling policies on multi-core systems

- Thank you!
- Questions?



- For more info: carey@cpsc.ucalgary.ca